

Fully Overwrapped Composite Pressure Vessels

An example

MAE 661 Laminated Composite Materials

Tank Requirements and Candidate Design

- Requirements
 - 305 mm diameter
 - Operating pressure of 20.7 MPa
 - Factor of safety of 2.0 against burst
 - Stress ratio at burst < 0.75
 - In service: ratio of operating pressure to yield pressure of 0.75
- Candidate design
 - Liner: 3.18 mm thick Al 6061-T6
 - $E = 68.9 \text{ GPa}$, $\nu = 0.33$, $\sigma_y = 290 \text{ MPa}$
 - Overwrap: AS4-3501-6 carbon/epoxy towpreg, $F_{1t} = 1830 \text{ MPa}$
 - Total hoop thickness $t_{90} = 2.54 \text{ mm}$
 - Total helical thickness $t_{30} = t_{-30} = 1.207 \text{ mm}$

Preliminary Calculations

- Since there is no bending deformation resulting from in-plane laminate loads, we want to trick CADEC into treating the laminate as symmetric; enter ply thicknesses accordingly, resulting in

$$[A] = \begin{bmatrix} 483151 & 148724 & 0 \\ 148724 & 659641 & 0 \\ 0 & 0 & 179200 \end{bmatrix} \text{MPa} \cdot \text{mm} \quad \text{Liner + Overwrap}$$

$$[A] = \begin{bmatrix} 237273 & 67585 & 0 \\ 67585 & 413762 & 0 \\ 0 & 0 & 89404 \end{bmatrix} \text{MPa} \cdot \text{mm} \quad \text{Overwrap only}$$

Before Liner Yields

- Apply a pressure of $p = 1 \text{ MPa}$ to the tank
 - In CADEC, apply

$$N_x = \frac{pr}{2} = \frac{\left(1 \frac{\text{N}}{\text{mm}^2}\right)(152.5\text{mm})}{2} = 76.25 \frac{\text{N}}{\text{mm}} \quad N_y = pr = \left(1 \frac{\text{N}}{\text{mm}^2}\right)(152.5\text{mm}) = 152.5 \frac{\text{N}}{\text{mm}}$$

to the liner + overwrap, and calculate fiber-direction stresses

- Results:

- In the aluminum, $\sigma_1 = 12.563 \text{ MPa}$, $\sigma_2 = 18.628 \text{ MPa}$, so

$$\sigma_{eq} = \sqrt{\sigma_1^2 - \sigma_1\sigma_2 + \sigma_2^2} = 16.456 \text{ MPa}$$

- In the $\pm 30^\circ$ plies, $\sigma_1 = 17.977 \text{ MPa}$
- In the 90° plies, $\sigma_1 = 30.266 \text{ MPa}$

- Determine the pressure at which the liner yields:

$$\frac{\sigma_y}{\sigma_{eq}} = \frac{290 \text{ MPa}}{16.456 \text{ MPa}} 1 \text{ MPa} = 17.62 \quad \text{so the liner yields when the pressure is } 17.62 \text{ MPa}$$

At Liner Yield

- At a pressure of 17.62 MPa, the fiber-direction stresses are:
 - In the $\pm 30^\circ$ plies, $\sigma_1 = 17.62 \times 17.977 \text{ MPa} = 316.75 \text{ MPa}$
 - In the 90° plies, $\sigma_1 = 17.62 \times 30.266 \text{ MPa} = 533.29 \text{ MPa}$
 - Additional capability of $1830 - 533.29 = 1296.71 \text{ MPa}$ in the hoop fibers
- As the pressure increases after the liner yields, all additional load goes into the composite
- We use CADEC to load up the composite only with additional pressure Δp (Δ denotes increment after liner yield)

After Liner Yield

- Apply a pressure $\Delta p = 1 \text{ MPa}$ to the composite only

$$N_x = \frac{\Delta p r}{2} = \left(1 \frac{N}{\text{mm}^2}\right) \frac{(152.5 \text{ mm})}{2} = 76.25 \frac{N}{\text{mm}} \quad N_y = \Delta p r = \left(1 \frac{N}{\text{mm}^2}\right) (152.5 \text{ mm}) = 152.5 \frac{N}{\text{mm}}$$

- Results:

- In the $\pm 30^\circ$ plies, $\Delta \sigma_1 = 36.98 \text{ MPa}$
- In the 90° plies, $\Delta \sigma_1 = 47.96 \text{ MPa}$

- The hoop fibers will fail at an incremental pressure of

$$\Delta p = 1 \text{ MPa} \frac{1296.71 \text{ MPa}}{47.96 \text{ MPa}} = 27.04 \text{ MPa}$$

or a total pressure of

$$p = 17.62 + 27.04 = 44.66 \text{ MPa}$$

- The total stresses in the fibers at failure:

- In the $\pm 30^\circ$ plies, $\sigma_1 = 316.75 + (27.04)(36.98) = 1317 \text{ MPa}$
- In the 90° plies, $\sigma_1 = 533.29 + (27.04)(47.96) = 1830 \text{ MPa}$

At Burst

- Burst factor of safety = (burst pressure)/(operating pressure)

$$FS = \frac{44.66MPa}{20.7MPa} = 2.16$$

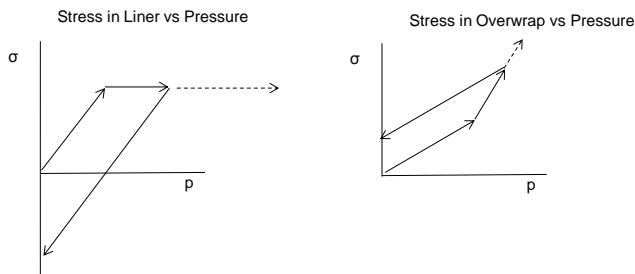
- Stress ratio at burst: (fiber direction stress in helicals)/(fiber direction stress in hoops)

$$SR = \frac{1317MPa}{1830MPa} = 0.72$$

- But the pressure at liner yield (17.62MPa) is less than the operating pressure (20.7MPa)

Proof Test

- To verify the quality of each tank, and to increase the liner yield pressure, the tanks are subjected to an intentional overpressure, or proof test



- Following the proof test to 4/3 of operating pressure, the liner is in compression and the overwrap is in tension.
- Upon reloading, the tank will not yield again until the proof pressure is reached.