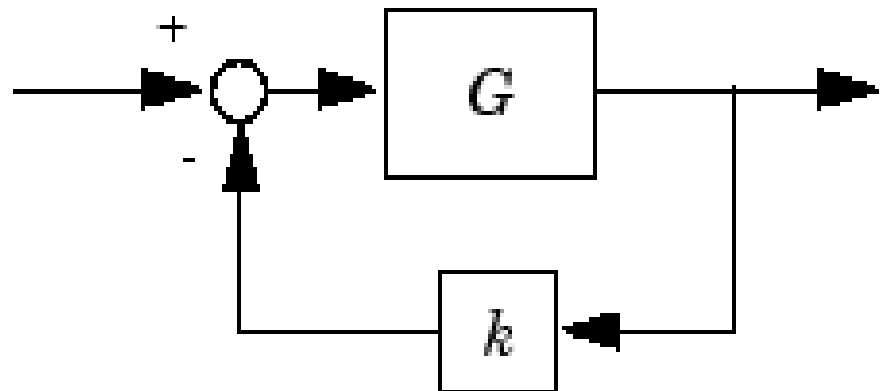


Stability, Gain Margins, Phase Margins

Stability Assessment for feedback

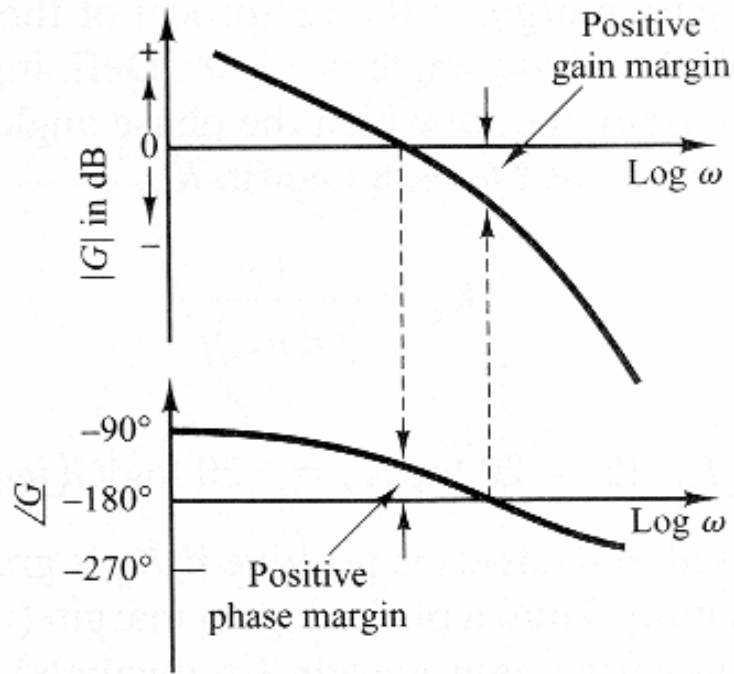
- Using Bode plots of the open-loop system, $G(s)$
- Characteristic equations $1+kG(s)=0$
- Based on Nyquist stability criteria



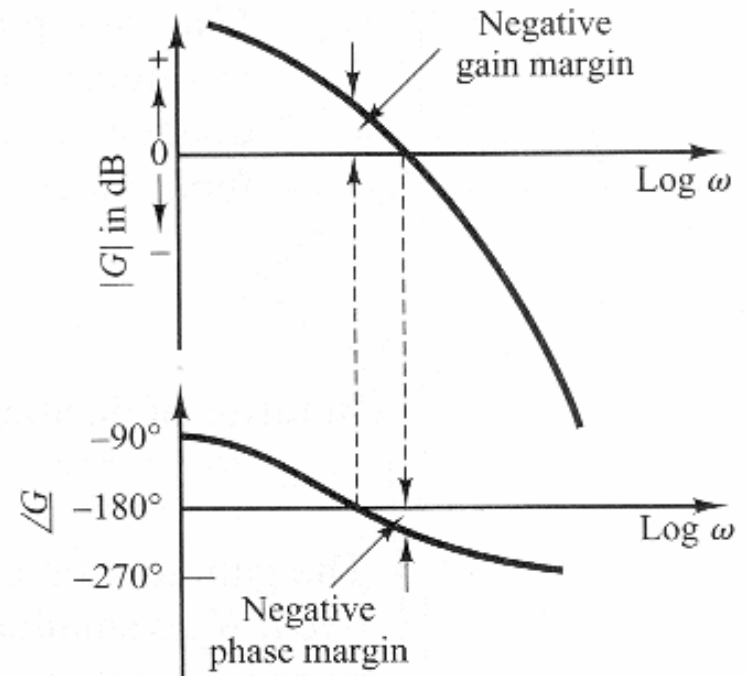
2 Criteria for feed back stability: Phase & Gain Margins

- $kG(s) = -1$
- Magnitude : 1 = 0 dB
- Phase: +/- 180 degrees
- Looking at the Bode plots of the open-loop system, $G(s)$
- Cross-over frequencies

Comparison of two



Stable system

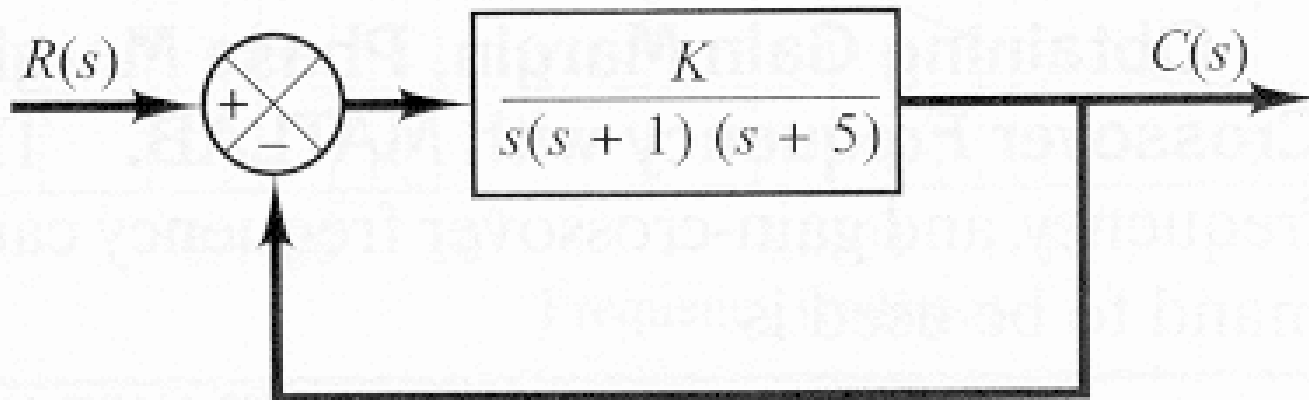


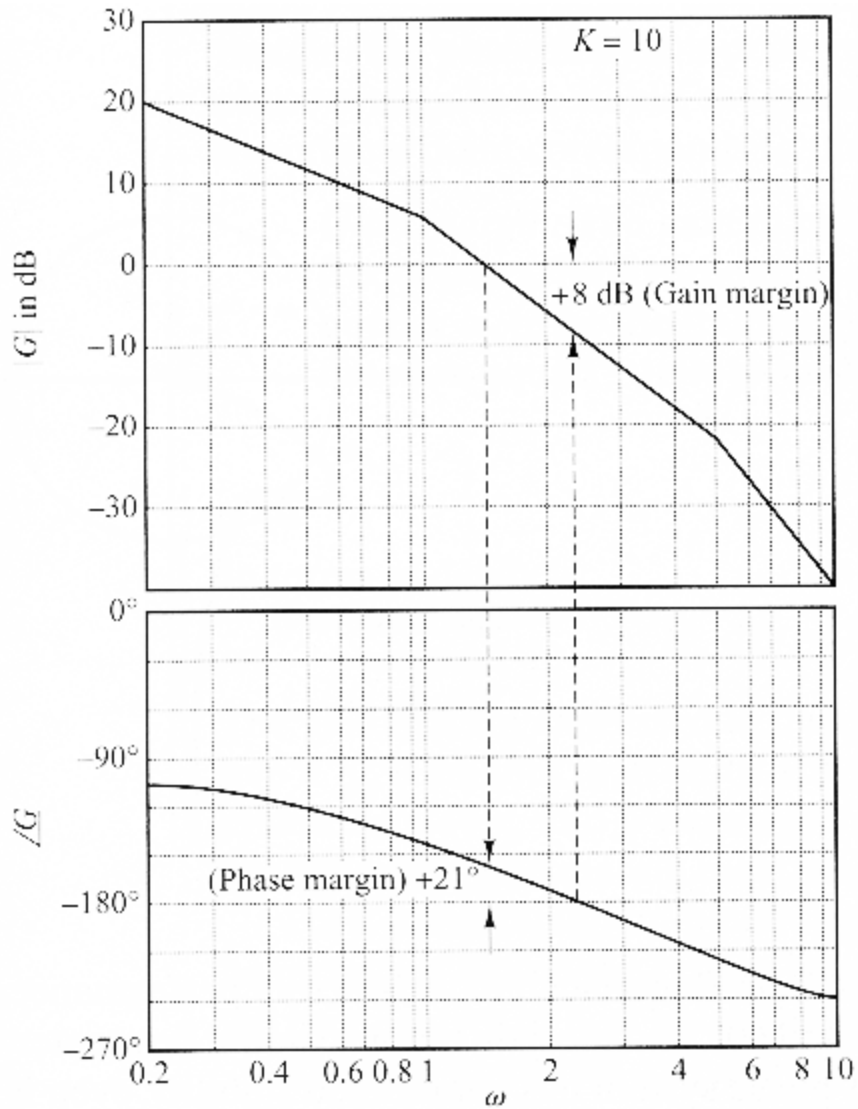
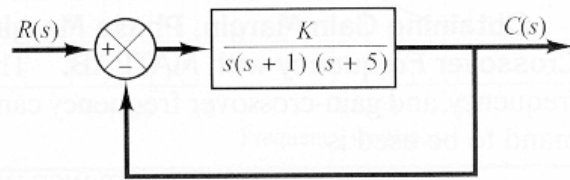
Unstable system

(a)

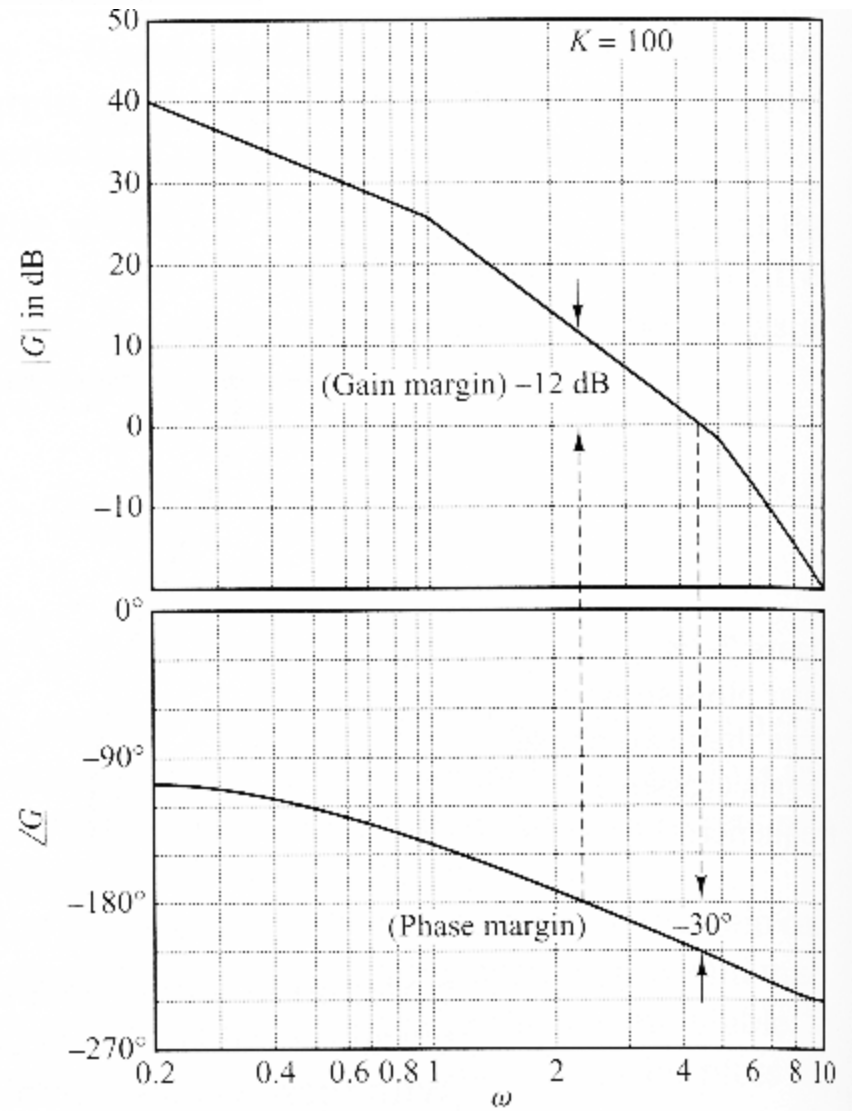
Example

$K = 10$ and $K = 100$.

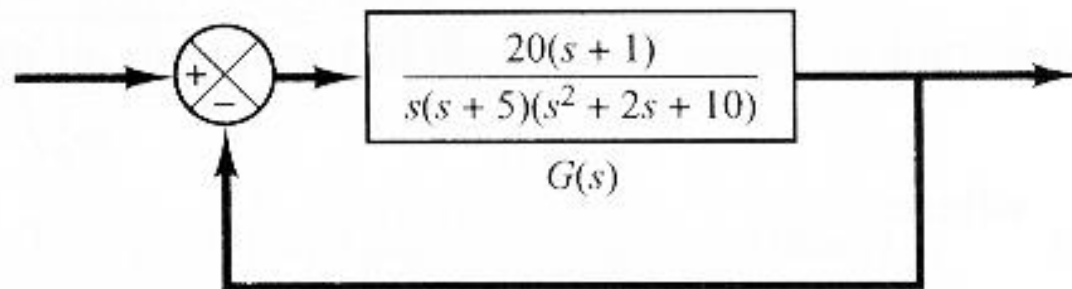




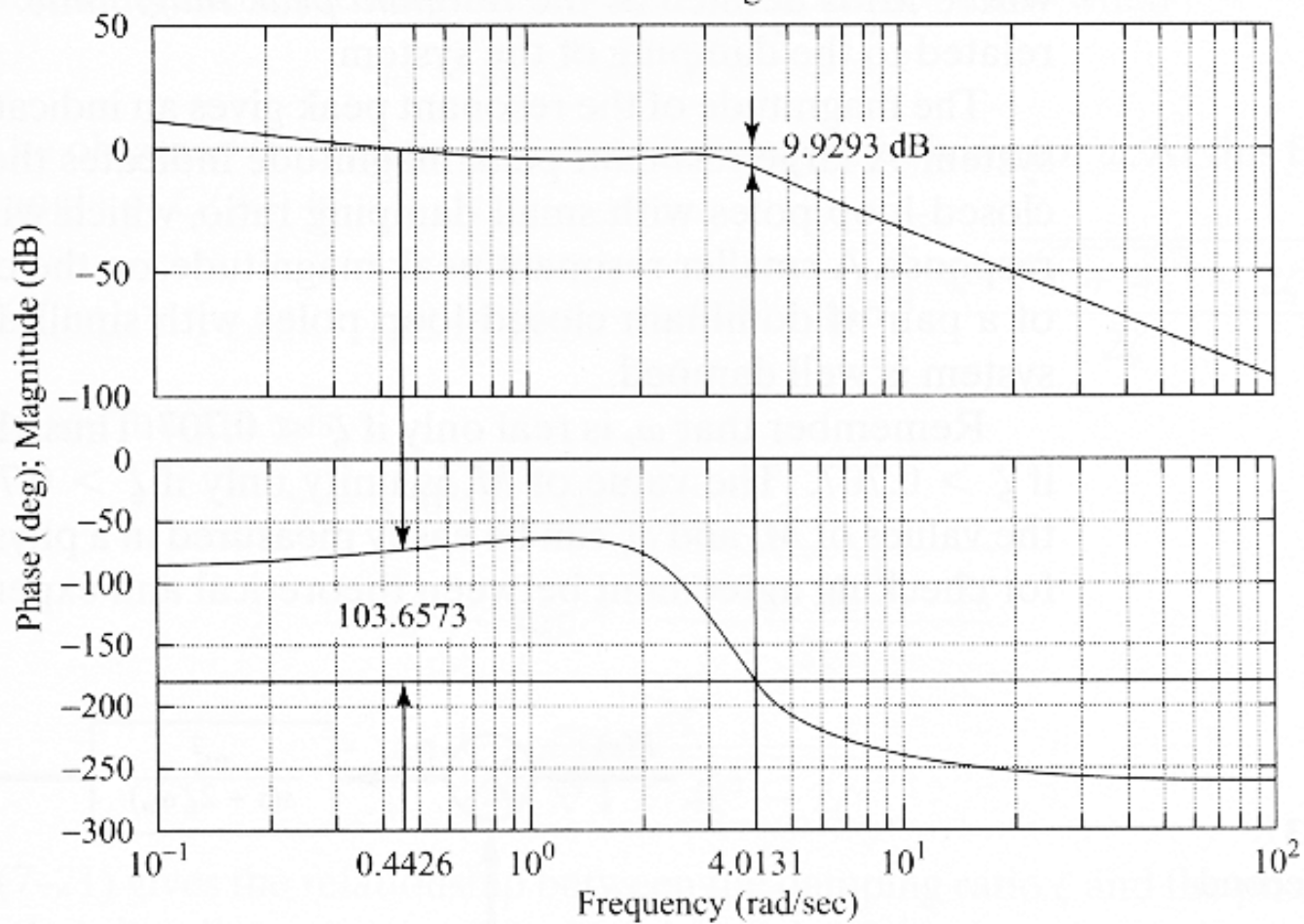
(a)



(b)



Bode Diagram



MATLAB : margin

MARGIN Gain and phase margins and crossover frequencies.

$[Gm, Pm, Wcg, Wcp] = \text{MARGIN}(\text{SYS})$ computes the gain margin Gm , the phase margin Pm , and the associated frequencies Wcg and Wcp , for the SISO open-loop model SYS (continuous or discrete).

The gain margin Gm is defined as $1/G$ where G is the gain at the -180 phase crossing.

The gain margin in dB is derived by $Gm_{dB} = 20 \cdot \log_{10}(Gm)$

The phase margin Pm is in degrees.

The loop gain at Wcg can increase or decrease by this many dBs before losing stability.

Matlab

```
num = [20 20];  
den = conv([1 5 0],[1 2 10]);  
sys = tf(num,den);  
w = logspace(-1,2,100);  
bode(sys,w)  
[Gm,pm,wcp,wcg] = margin(sys);  
GmdB = 20*log10(Gm);  
[GmdB pm wcp wcg]
```

```
ans =
```

```
9.9293 103.6573 4.0131 0.4426
```

End